

# A Kinetic Study of Opinion Dynamics in Multi-Agent Systems

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# Introduction

## Opinion Evolution

Opinion evolution in a multi-agent system is modeled using a **kinetic** approach.

## Sociophysics

- Kinetic theory of gases describes the effects of interactions among molecules in a gas from a microscopic viewpoint.
- By reinterpreting the molecules of a gas as agents, one can use the kinetic framework to describe social interactions in a multi-agent system.

# Microscopic Model

## Binary Interactions

The opinions of two interacting agents change according to

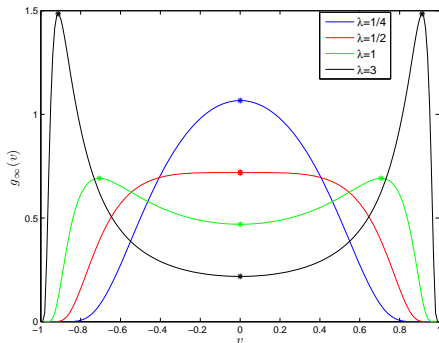
$$\begin{cases} v' = v + \gamma C(|v|)(w - v) + \eta_* D(|v|) \\ w' = w + \gamma C(|w|)(v - w) + \eta D(|w|) \end{cases} \quad (1)$$

where

- $(v', w')$  are the post-interaction opinions of the two agents whose pre-interaction opinions are  $(v, w)$ ;
- $\gamma \in (0, 1/2)$ ;
- $\eta$  and  $\eta_*$  are two independent random variables with distribution function  $\vartheta(\cdot)$ ;
- $C(\cdot)$  is the compromise function ( $C(|v|) = 1$ );
- $D(\cdot)$  is the diffusion function ( $D(|v|) = 1 - v^2$ ).

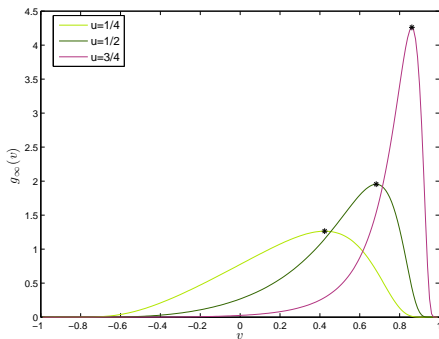
$u=0$

- $u$ : average opinion;
- $v$ : opinion;
- $g_{\infty}(v)$ : stationary profile;
- $\lambda$ : constant related to compromise and diffusion.



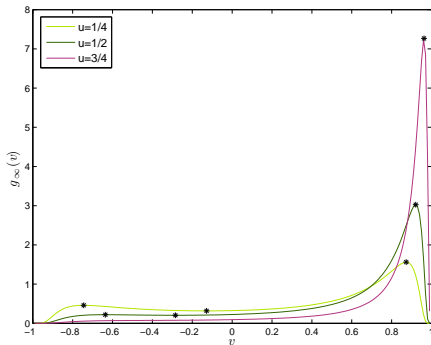
$$\lambda = 1/4$$

- $u$ : average opinion;
- $v$ : opinion;
- $g_{\infty}(v)$ : stationary profile;
- $\lambda$ : constant related to compromise and diffusion.



$$\lambda = 3/2$$

- $u$ : average opinion;
- $v$ : opinion;
- $g_{\infty}(v)$ : stationary profile;
- $\lambda$ : constant related to compromise and diffusion.



# Thank you for your attention

Simulations of Opinion Formation in  
Multi-Agent Systems using Kinetic Theory

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